Master's Thesis

Acceleration of Hyperparameter Learning via $\ell_p\text{-bilevel}$ Optimization Problems

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Abstract

We focus on tackling the problem of hyperparameter tuning in the ℓ_p -regularization optimization model for machine learning tasks. One of the natural ways is to formulate the problem into a bilevel optimization problem where decision valuables include hyperparameters, its objective function reflects the predictive performance of the model, and the lower-level optimization problem is the original machine learning model with the hyperparameters. The existing method adopts the smoothing approach to transform the ℓ_p -regularization term into a differentiable function. Then using the Karush-Kuhn-Tucker conditions, the differentiable bilevel optimization problem becomes a solvable single-level optimization problem. Such a method has good interpretability, but it must be time-consuming for large-scale learning tasks with a large sample set. To overcome this issue, we propose reducing the sample size based on the dual sparse model used in the support vector regression. By combining a grid search of sample size with bilevel smoothing optimization, we propose a method that can tune the hyperparameters of a model while excluding the influence of irrelevant samples. Numerical experiments demonstrate that our proposed method significantly reduces computation time.